

Computer Science II

Environmental Engineering Second Level 2024-2025 1st Course

Lecture #4

Programming with MATLAB (Cont.)

13. MATRICES

Matrices are the basic elements of the MATLAB environment. A matrix is a two-dimensional array consisting of m rows and n columns. Special cases are column vectors ($n = 1$) and row vectors ($m = 1$).

In this section we will illustrate how to apply different operations on matrices. The following topics are discussed: vectors and matrices in MATLAB, the inverse of a matrix, determinants, and matrix manipulation.

13. MATRICES (Cont.)

MATLAB supports two types of operations, known as matrix operations and array operations. Matrix operations will be discussed first.

End as a subscript to access the last element of a matrix along a given dimension use end as a subscript.

13. MATRICES (Cont.)

Entering a vector:

A vector is a special case of a matrix. The purpose of this section is to show how to create vectors and matrices in MATLAB. As discussed earlier, an array of dimension $1 \times n$ is called a row vector, whereas an array of dimension $m \times 1$ is called a column vector. The elements of vectors in MATLAB are enclosed by square brackets and are separated by spaces or by commas.

13. MATRICES (Cont.)

Entering a vector (Cont.):

For example, to enter a row vector, v, type:

```
>> v = [1 4 7 10 13]
```

```
v =
```

```
1 4 7 10 13
```

13. MATRICES (Cont.)

Entering a vector (Cont.): For example, to enter a row vector, v, type:

```
>> v = [1 4 7 10 13]
```

```
v = 1 4 7 10 13
```

Column vectors are created in a similar way, however, semicolon (;) must separate the components of a column vector,

```
>> w = [ 1; 4; 7; 10; 13] → w = 1
```

```
4
```

```
7
```

```
10
```

```
13
```

13. MATRICES (Cont.)

Entering a vector (Cont.):

On the other hand, a row vector is converted to a column vector using the transpose operator. The transpose operation is denoted by an apostrophe or a single quote (').

>> w = v' → w = 1

4

7

10

13

13. MATRICES (Cont.)

Colon operator in a matrix :

The colon operator can also be used to pick out a certain row or column. For example, the statement $A(m : n, k : l)$ specifies rows m to n and column k to l .

Subscript expressions refer to portions of a matrix. For example,

```
A = 1  2  3
```

```
     4  5  6
```

```
     7  8  0
```

```
>> A(2, :)
```

```
ans = 4  5  6
```

 is the second row elements of A.

13. MATRICES (Cont.)

Colon operator in a matrix (Cont.) :

The colon operator can also be used to extract a sub-matrix from a matrix A.

```
>> A( : , 2:3 )
```

```
ans = 2 3
```

```
5 6
```

```
8 0
```

$A(: , 2:3)$ is a sub-matrix with the last two columns of A.

A row or a column of a matrix can be deleted by setting it to a null vector, [].

```
>> A( : , 2) = [ ] → ans = 1 3
```

```
4 6
```

```
7 0
```

13. MATRICES (Cont.)

Creating a sub-matrix:

To extract a submatrix B consisting of rows 2 and 3 and columns 1 and 2 of the matrix A, do the following:

```
>> B = A ( [2 3], [1 2] )
```

```
B = 4    5
```

```
7    8
```

To interchange rows 1 and 2 of A, use the vector of row indices together with the colon operator.

13. MATRICES (Cont.)

Creating a sub-matrix (Cont.):

```
>> C = A ([2 1 3], :)
```

```
C = 4 5 6
```

```
1 2 3
```

```
7 8 0
```

It is important to note that the colon operator (:) stands for all columns or all rows. To create a vector version of matrix A, do the following:

13. MATRICES (Cont.)

Creating a sub-matrix (Cont.):

```
>> A ( : ) → ans = 1
```

4

7

2

5

8

3

6

0

13. MATRICES (Cont.)

Creating a sub-matrix (Cont.):

The submatrix comprising the intersection of rows p to q and columns r to s is denoted by $A(p:q,r:s)$.

As a special case, a colon ($:$) as the row or column specifier covers all entries in that row or column; thus:

- $A(:,j)$ is the j th column of A , while
- $A(i,:)$ is the i th row, and
- $A(\text{end},:)$ picks out the last row of A .

13. MATRICES (Cont.)

Creating a sub-matrix (Cont.):

The keyword `end`, used in `A(end,:)`, denotes the last index in the specified dimension. Here are some examples.

```
>> A(2:3, 2:3) → ans = 5 6  
                        8 9
```

```
>> A(end:-1:1, end)
```

```
ans = 9
```

```
6
```

```
3
```

13. MATRICES (Cont.)

Creating a sub-matrix (Cont.):

```
>> A( [1 3] , [2 3] )
```

```
ans = 2 3
```

```
8 9
```

Ex:-

```
>> q = 4:10
```

```
q = 4 5 6 7 8 9 10
```

```
>> q (end)
```

```
ans = 10
```


13. MATRICES (Cont.)

Creating a sub-matrix (Cont.):

```
>> q(end-2 : end)
```

```
ans = 8 9 10
```

Thus, $v(1)$ is the first element of vector v , $v(2)$ its second element, and so forth.

Furthermore, to access blocks of elements, we use MATLAB's colon notation (:).

For example, to access the first three elements of v , we write,

```
>> v (1 : 3)    →  ans = 1  4  7
```

13. MATRICES (Cont.)

Creating a sub-matrix (Cont.):

Or, all elements from the third through the last elements,

```
>> v(3:end) → ans = 7 10 13
```

where end signifies the last element in the vector. If v is a vector, writing

```
>> v(:)
```

produces a column vector, whereas writing

```
>> v(1:end)
```

produces a row vector.

13. MATRICES (Cont.)

Creating a sub-matrix (Cont.):

Or, all elements from the third through the last elements,

```
>> v(3:end) → ans = 7 10 13
```

where end signifies the last element in the vector. If v is a vector, writing

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